

Tangible Images of Real Life Scenes

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Abstract

Haptic technologies allow for adding a new “touching” modality into virtual scenes. However, 3D reconstruction of real life scene often results in millions of polygons which cannot be simultaneously visualized and haptically rendered. In this paper, we propose a way of haptic interaction with the reconstructed real life scenes where multiple original images of the real scenes are augmented with the reconstructed polygon meshes. We present our solution to the problems of haptic model alignment with the images and interactive haptic rendering of large polygon meshes with reconstruction artifacts. In particular, the presented collision detection algorithm is not restricted by any hypothesis and robust enough to support smooth interaction with millions of polygons. The feasibility and usability of the proposed solution is evaluated in a user study.

Keywords:

haptic interaction; tangible image; large-scale imperfect polygon mesh

1. Introduction

Haptic technology, or haptics, is an interaction feedback technology based on applying forces, vibrations, and/or motions to the user. Usually, haptic interaction is considered with 3D objects defined by polygons. However, 3D reconstruction of a real life scene using computer vision techniques often results in millions of polygons which cannot be simultaneously visualized and haptically rendered. Mesh simplification methods and acceleration techniques can help, however in many cases the visual display of a photorealistic scene still creates a very significant and time consuming overhead to the whole project implementation pipeline. Replacement of the actual 3D scenes with their images is actively used in image-driven visualization such as interactive panoramas, street walkthroughs, and online shopping with interactive images. Similarly, replacement of the interactive 3D scenes with their “tangible images” is an alternative solution to this problem.

Haptic interaction with images, as if they were actual 3D scenes, can be done in a few different ways, which were also previously explored: Firstly, the haptic forces can be derived directly from the image by analyzing pixel intensity [1]. This approach, however, imposes restrictions on the scene illumination. Secondly, haptic components can be added to the images and used for haptic interaction by sketching simplified haptic models on the image so that the models were eventually matched with the respective parts of the displayed scene [2]. Thirdly, in case when there are available reconstructed polygon meshes, they can be also

matched with the image and only used for haptic interaction while the original image is displayed thus liberating the computer from 3D visualization task. We proposed our initial solution to this problem in [3] where we mostly worked on the haptic rendering algorithm for large and imperfect polygon meshes.

In this paper we continue this research solving a problem of haptic interaction with the reconstructed real life scenes where *multiple original images of the real scenes* are augmented with the reconstructed polygon meshes. This required us to solve problems of haptic model alignment with multiple images to be displayed as well as smooth interactive haptic rendering of large multi-million polygon meshes, which may have inevitable reconstruction artifacts.

In Section II, we survey the relevant works. In Section III, we discuss the overall project pipeline, describing how to match the reconstructed mesh with the image and how to perform haptic interaction with large-scale imperfect meshes. Results of the proposed algorithm are provided in Section IV. The design and evaluation of the usability test is presented in Section V to prove the feasibility and usefulness of the presented tangible images approach, followed by the conclusion in Section VI.

2. Related Work

2.1. Visual Rendering in a Visual-haptic Interaction Environment

In a visual-haptic interactive scene, polygon meshes, as well as the haptic cursor, are usually displayed for visual feedback. Haptic rendering on large meshes is discussed in section 2.3. In this section we talk about the problem in visual rendering, which is that even if the large mesh can be

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63 haptically and visually rendered, displaying haptic cursor
 64 along with the mesh is problematic. The reason is given in
 65 the next paragraph.

66 The haptic cursor position is computed by the CPU
 67 (together with other haptic rendering tasks) at the rate of 1
 68 kHz. In each graphics frame (30-60 Hz), the cursor position
 69 is read from the haptic callback function for visual display
 70 of the cursor. Thus samples of cursor position are displayed
 71 at graphics update rate. As we know, the graphics rendering
 72 time increases with increasing mesh size. This would in
 73 turn lead to an increase in sampling interval of cursor
 74 position (as in Fig. 1), resulting in clumsiness in the
 75 displayed cursor movement. To reduce the graphics
 76 rendering time for visual models, we need to either speed
 77 up the rendering process or to reduce the size of the models.

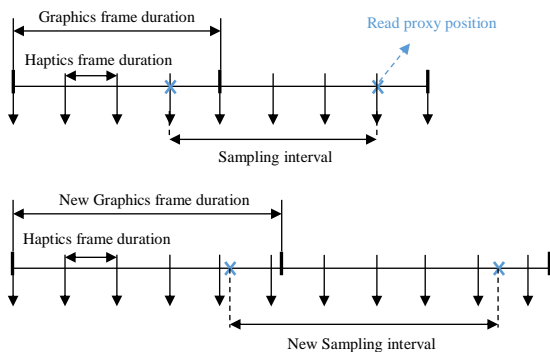


Fig. 1. Illustration of the effect of increasing graphics rendering time in one frame. Sampling interval is always equal to the graphics frame duration. We need to keep the sampling interval small in order to display the haptic cursor consistently.

78 Common graphical renderers in visual-haptic
 79 interaction, such as OpenGL and Direct3D, utilize
 80 rasterization-based rendering due to the real-time
 81 requirement. With powerful graphics hardware and the use
 82 of acceleration structures for culling, a complex interactive
 83 scene can be rendered in real-time. However, the level of
 84 realism of the rendered scene heavily depends on the
 85 lighting techniques applied to the scene and the manual
 86 efforts of designers, which poses an obstacle to realistic
 87 immersion. Compared to rasterization-based algorithms,
 88 ray tracing provides a more realistic visual effect, but it is
 89 costly in computation. With the emergence of high-
 90 performance rendering engines like Brigade [4], it has
 91 become possible to incorporate ray tracing into real-time
 92 rendering. However, it is still far from being applied in
 93 interactive visual-haptic scenes with millions of polygons.

94 In order to display a more realistic scene, there are
 95 works combining ray tracing with rasterization-based
 96 rendering in a visual-haptic interaction environment. For
 97 example, Morris and Joshi propose to display pre-processed
 98 raytraced images to simulate a static-viewpoint scene [5].
 99 Depth information is extracted here along with the image
 100 for proper occlusion with other objects rendered in real-
 101 time. In this way, costly computation is avoided in the
 102 rendering loop and visual realism is improved.

103 Based on previous work [5], we know that images can
 104 be a promising alternative to displaying the models in some
 105 real-time applications. For real life scenes, images provide
 106 high-resolution visual feedback without complex
 107 computations.

108 2.2. Haptic Interaction with Images

109 Methods for haptic interaction with images can be
 110 roughly categorized into two groups. The first group of
 111 methods generate force feedback based on image
 112 processing techniques. They first build a correspondence
 113 between the derived image properties (e.g., grayscale or
 114 color values of the pixels) and the model (e.g., depth map
 115 or 2.5D geometry model) for force calculation, and then
 116 compute the force on-the-fly. These methods allow us to
 117 feel the object edges and textures as well as its visible
 118 geometry in certain cases. The whole image scene is,
 119 however, perceived tangibly only as an embossment of the
 120 relief. Besides, since none of the properties can always
 121 represent the actual scene geometry of any image, these
 122 techniques can only be applied to a specific group of images
 123 (e.g., frontally illuminated images).

124 The second group of methods augments images with
 125 haptic models matching the image content. In this way, the
 126 users are allowed to perceive the full 3D geometry of the
 127 objects in the images, including the invisible surfaces. The
 128 augmented models can be geometry models, depth maps, or
 129 even mathematical functions and procedures [6-7].

130 High requirement for haptic refresh rate, however,
 131 imposes a constraint on the computation time. If we want
 132 to use polygon model in the interaction, we need to make a
 133 tradeoff between the complexity of the polygon model and
 134 the continuity of the force feedback. Some methods use
 135 simplified meshes to meet the real-time requirement and
 136 provide additional information to simulate haptic details on
 137 the surface. For example, M. A. Otaduy et al. [6] extract 3D
 138 texture-induced force from texture images and apply it
 139 along with low-resolution geometry-induced force. Kim et
 140 al. [8] propose to define geometric information as a depth
 141 map while stiffness and viscosity maps are applied at the
 142 same time to represent physical properties of the scene. To
 143 avoid the constraint, there are also methods that resort to
 144 other geometry representation. In our previous paper [2],
 145 we define the basic geometry of the models using FRep
 146 models (variants of implicit functions) and add texture
 147 force to simulate details. All these methods allow the users
 148 to perceive the haptic details to some extent, but none of
 149 them manage to tangibly present the high-fidelity geometry
 150 of the objects in real life images.

151 Multi-view reconstruction methods such as MVE [9]
 152 are able to produce polygon meshes of a complex scene
 153 which are sufficient for visualization. If we use the
 154 reconstructed model to provide haptic feedback for the
 155 images served as input in the reconstruction pipeline, the
 156 haptic display could be easily registered with the images. In
 157 this way, a high-resolution haptic feedback can be achieved
 158 we are able to deliver a realistic haptic immersion into
 159 images as if they were 3D scenes. Therefore, if we could
 160 find a way to handle collision detection with reconstructed
 161 meshes, a reconstructed model is an ideal choice for the
 162 haptic interaction with images.

163 2.3. Point-based Haptic Rendering with Polygon Meshes

164 The challenge of collision detection with large-scale
 165 meshes lies in locating the polygon that the haptic cursor
 166 (Haptic Interface Point, HIP) is in contact with in real-time.
 167 We call it the *active polygon* in this paper. In a virtual scene,
 168 a *proxy* is calculated to indicate the position of HIP. When
 169 the HIP moves in the free space, the proxy position matches

170 with the position of the HIP. When the HIP collides with
 171 the mesh, i.e. inside the mesh, if it is a simulation of rigid-
 172 to-rigid collision, the proxy lies on the surface of the active
 173 polygon.

174 Many existing methods for haptic rendering of polygon
 175 meshes detect collision with the whole polygon mesh in
 176 each haptic frame. The haptic rendering time thus depends
 177 on the number of polygons. For example, in widely-used
 178 haptic rendering methods such as God-Object [10], Ruspini
 179 [11] and CHAI3D [12], active constraint polygons need to
 180 be found first from all the polygons in each haptic frame,
 181 and then the constraint polygon with the shortest distance
 182 to the haptic cursor is determined as the active polygon.
 183 OpenHaptics HLAPI [13] utilizes the OpenGL Depth
 184 Buffer and Feedback Buffer to access shapes rendered in
 185 graphics rendering loop and automatically detect collision
 186 based on the geometry and depth information stored inside
 187 these two buffers. In this way, HLAPI’s performance is not
 188 influenced by the size of polygons. However, the Feedback
 189 Buffer has a limited size (storing up to 65536 vertices) and
 190 using the Depth Buffer results in discontinuities in the
 191 computed haptic force due to the fact that 3D geometry is
 192 saved as an image in the Depth Buffer.

193 There are a number of methods that have been proposed
 194 to reduce the computational time using spatial partitioning
 195 and hierarchical structures, such as H-COLLIDE [14] and
 196 ActivePolygon [15]. In the ActivePolygon algorithm,
 197 polygons are stored in an octree data structure. Only the
 198 polygons stored in the cells that the haptic cursor passes by
 199 between frames are used for collision detection. These
 200 methods could effectively reduce the haptic rendering time,
 201 however, they cannot handle the situation when the mesh is
 202 too dense, because the computation complexity of these
 203 algorithms depends on the number of polygons in the cells
 204 that the haptic cursor passes from frame-to-frame. Thus, if
 205 the haptic cursor moves very fast and passes several cells
 206 within one cycle, only the first cell (obtained from the
 207 cursor position in last frame) and the last cell (obtained
 208 from the cursor position in current frame) are known while
 209 the in-between cell information is lost. To avoid missing the
 210 active polygon, all the cells that the cursor might pass need
 211 to be considered and this would lead to a significant
 212 expansion in the search range, even if the cell size is
 213 optimized. For example, the maximum velocity of the
 214 Geomagic Touch desktop haptic device is 2.5 mm/ms, so
 215 all the polygons in those cells within the distance of 2.5 mm
 216 to the previous position of haptic cursor need to be checked.
 217 If the mesh is dense and has a few hundred polygons within
 218 a 2.5 mm cubic space, fast and accurate collision detection
 219 cannot be maintained.

220 Geometry connectivity information was first used by
 221 Chih-Hao Ho et al. in their “neighborhood watch”
 222 algorithm [16] to predict the next active primitive (an
 223 extension of active polygon) based on the previous active
 224 primitive. It refers to the vertex, line segment or polygon
 225 that the haptic cursor is in contact with. Before haptic
 226 rendering, the connectivities among vertices, lines and
 227 polygons of the mesh are predefined and stored. After the
 228 first collision is detected, only the neighbors of the previous
 229 active primitive are checked. Using an iterative approach
 230 one can track the trace of the haptic cursor and find the
 231 closest primitive at the current position. In this way, the

232 haptic rendering time is independent of the number of
 233 polygons except for every first collision with the mesh.

234 Inspired by the “neighborhood watch” algorithm [16],
 235 we propose a hybrid collision detection method which
 236 combines the pre-computed connectivity information and
 237 spatial partitioning. Instead of directly searching for the
 238 active primitive, we first track the polygon intersected with
 239 HIP trace and then use it as start point to track the active
 240 primitive. In this way, the computational time is fully
 241 independent of the polygon number. One of the main
 242 differences between our proposed method and Chih-Hao
 243 Ho’s method is that we are not dealing with perfect CAD
 244 polygon meshes. The geometry information obtained from
 245 the meshes can be incomplete, may contain redundant
 246 vertices and facets, or may even be wrong. Thus more
 247 general criteria for searching for the active primitive is
 248 needed.

249 3. Making Tangible Images

250 Augmenting images with haptic models requires for
 251 answering two questions: where to obtain the
 252 corresponding models and how to match them with the
 253 respective parts of the images.

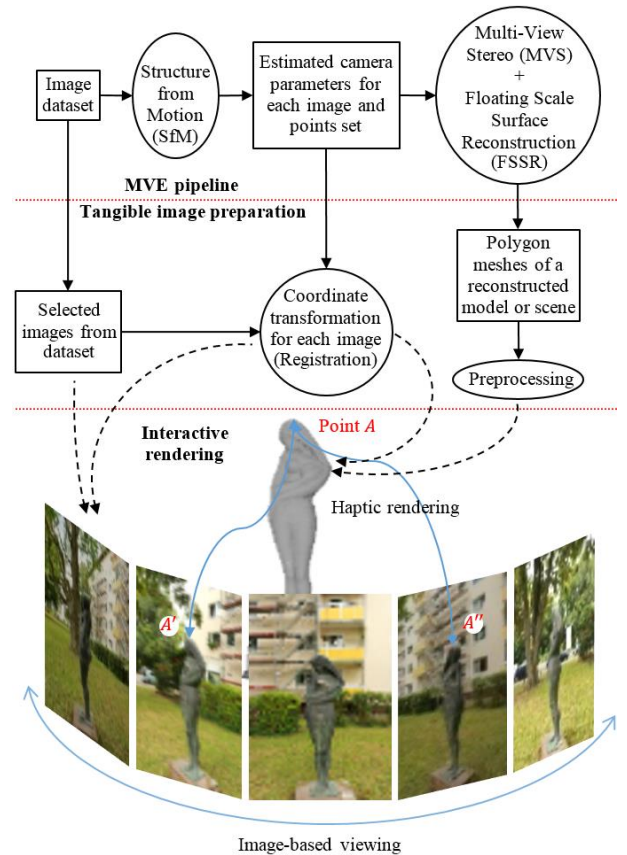


Fig. 2. In the MVE pipeline, Structure-from-Motion (SfM) techniques are used to reconstruct camera parameters and a sparse points set. Then a mesh is reconstructed using Multi-View Stereo (MVS) and Floating Scale Surface Reconstruction (FSSR) approach. In tangible image pipeline, the reconstructed model is matched with corresponding images to provide haptic feedback. Rotation of the scene can be simulated by a series of selected images.

254 There are several ways to obtain models of a real scene,
 255 such as interactive modeling of the scene in computer-aided
 256 design systems, reproducing the model based on the data

257 collected from 3D scanners and reconstructing the model
 258 based on multi-view reconstruction methods. Matching a
 259 model with an image requires for taking into account its
 260 perspective distortions: we may either define the model in
 261 a perspectively distorted modeling space matching the
 262 image coordinate space as in [2], or use camera projection
 263 transformation for mapping coordinates between the image
 264 and the model coordinate spaces.

265 In this paper, we use reconstructed models to make the
 266 corresponding image dataset tangible. Models generated
 267 from MVE [9] are used as examples. Given multiple images
 268 of a real scene, MVE reconstructs a polygon mesh of the
 269 scene, along with the estimated camera parameters for each
 270 input image (as shown in the MVE pipeline in Fig. 2). If the
 271 input image dataset contains close-up photos, the output can
 272 be a high-resolution 3D scene with millions of polygons
 273 and some regions are of a higher resolution than other parts.

274 In the pipeline of tangible image (as illustrated in Fig.
 275 2), we simulate virtual walkthroughs in the real scene with
 276 a series of selected images from the dataset. Then the
 277 reconstructed model is registered with each image using the
 278 estimated camera parameters and the respective coordinate
 279 transformation. To incorporate reconstructed meshes in
 280 haptic interaction, the worst case scenario is considered in
 281 this paper, i.e. we show an approach to haptically rendering
 282 large-scale imperfect meshes. This approach is pluggable
 283 and can be used for haptic rendering with any large-scale
 284 meshes. It performs the following tasks:

- 285 • **Coordinate transformation.** We register the
 286 haptic display with the photo using the
 287 reconstructed camera parameters.
- 288 • **Preprocessing.** We deal with the imperfections of
 289 the reconstructed mesh and build acceleration
 290 structures for collision detection.
- 291 • **Haptic rendering.** We propose a hybrid collision
 292 detection algorithm to handle collision detection
 293 with large-scale meshes and explain how to render
 294 force feedback based on the collision results.

295 3.1. Coordinate transformation

296 When using images to replace visual rendering of the
 297 meshes, we need to match the haptic models with the
 298 images so that the image content matches the haptic display.
 299 In a multi-view reconstruction process, camera parameters
 300 of the images can be estimated based on structure-from-
 301 motion techniques [17]. Therefore, given a target image and
 302 corresponding reconstructed model, the estimated camera
 303 parameters could be used to calculate the *modelview* and
 304 *projection* matrices for projecting the model in the camera
 305 frustum. Suppose R_C is the orientation matrix of the virtual
 306 camera with respect to the world coordinate system, T_C
 307 is the column vector which defines the location of the virtual
 308 camera in the world coordinate system, f is the focal length
 309 of the camera, img_width and img_height are the width and
 310 the height of the given image, pp_x and pp_y are x , y
 311 coordinates of the principal point offset of the camera in
 312 pixel coordinate system, z_{near} and z_{far} are the z coordinates
 313 of the near and far clipping planes, then the 4*4 modelview
 314 and projection matrices M_{mol} and M_{proj} can be obtained as
 315 follows:

$$316 \quad M_{mol} = \begin{pmatrix} R_C & T_C \\ 0 & 1 \end{pmatrix} \quad (2)$$

$$317 \quad M_{proj} = \begin{pmatrix} 2f\alpha_x & 0 & 2(pp_x - 0.5) & 0 \\ 0 & 2f\alpha_y & 2(pp_y - 0.5) & 0 \\ 0 & 0 & \frac{z_{far}+z_{near}}{z_{far}-z_{near}} & \frac{-2z_{far}z_{near}}{z_{far}-z_{near}} \\ 0 & 0 & 1 & 0 \end{pmatrix} \quad (3)$$

$$318 \quad aspect = img_width/img_height \quad (4)$$

$$319 \quad \alpha_x = \begin{cases} 1, & \text{if } aspect > 1 \\ 1/aspect, & \text{if } aspect \leq 1 \end{cases} \quad (5)$$

$$320 \quad \alpha_y = \begin{cases} aspect, & \text{if } aspect > 1 \\ 1, & \text{if } aspect \leq 1 \end{cases} \quad (6)$$

321 Note that the origin of the image coordinate system for
 322 the MVE-produced models is at the top-left corner of the
 323 image while it is at the bottom-left corner of the image in
 324 OpenGL. Therefore when displaying MVE models in
 325 OpenGL, the y-axis needs to be inverted to match the
 326 image. This could be done by inverting all elements in the
 327 second row of either M_{mol} or M_{proj} .

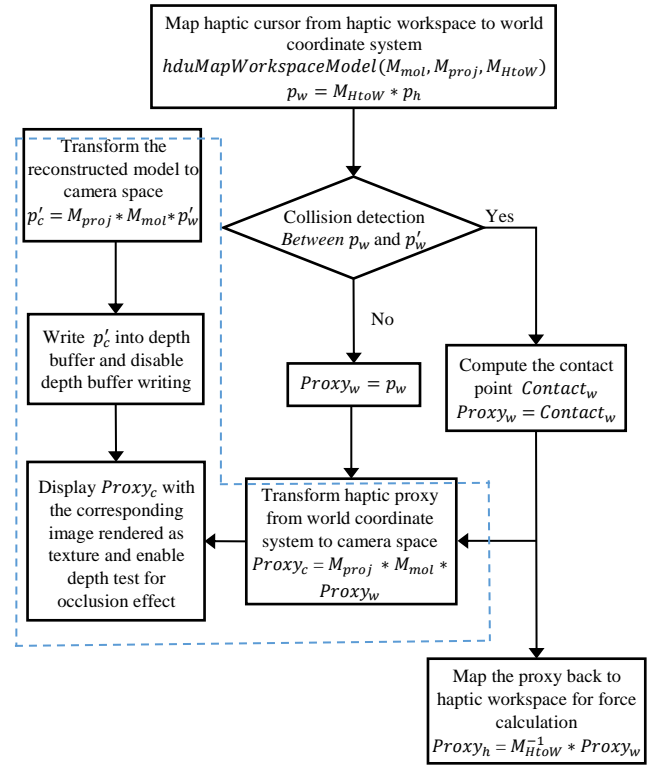


Fig. 3. Flowchart of the mapping process.

328 There are three workspaces involved in the visual-
 329 haptic interaction: the camera workspace (defined during
 330 the structure-from-motion process), the haptic workspace,
 331 and the world coordinate system. The whole mapping and
 332 transformation process behind the interaction scene is
 333 illustrated in the flowchart in Fig. 3. The procedures
 334 enclosed by the blue dashed lines are for visual rendering.
 335 In real 3D scenes, the haptic cursor would be hidden when
 336 moving to the back of the objects. To simulate such
 337 occlusion effect with displaying only 2D images, we write
 338 the reconstructed models to the depth buffer and then
 339 disable writing to the depth buffer right after the writing
 340 operation. The depth buffer writing is kept disabled in the

341 following rendering loop. Afterwards, with depth test
 342 enabled and *glDepthFunc* depth comparison function set to
 343 `GL_LEQUAL`, the depth values of the models rendered in
 344 real-time (e.g., haptic cursor) are compared with the depth
 345 values stored in the depth buffer. A pixel of the haptic
 346 cursor is only drawn if the incoming depth value at this
 347 pixel is less than or equal to the stored depth value. In such
 348 a way, if the haptic cursor goes to the back of the
 349 reconstructed model (i.e. the incoming depth value is
 350 greater than the stored depth value), it is not drawn and the
 351 occlusion effect is thus achieved.

352 In the haptic servo loop thread, the position of the haptic
 353 cursor is mapped to the world coordinate system for
 354 collision detection and then mapped back to the haptic
 355 workspace for force rendering if the collision happens. The
 356 generated proxy position is transformed to the camera
 357 workspace and sent to the client thread for displaying.

358 3.2. Preprocessing of the reconstructed mesh

359 In order to apply the collision detection algorithm, we
 360 need to preprocess the reconstructed mesh, which includes
 361 three steps.

362 The first step is to handle imperfections with regard to
 363 duplicate vertices inside the mesh. Reconstructed models
 364 are likely to have duplicate vertices, e.g., the city wall
 365 model in Fig. 9(a) has 1883 groups of duplicate vertices.
 366 These vertices cause the appearance of holes during haptic
 367 rendering leading to pop-throughs during the haptic
 368 interaction. We therefore delete the duplicate vertices and
 369 zero-area polygons in the mesh in the following way. All
 370 the vertices are traversed to form a list of duplicate vertex
 371 groups, and in each group the vertex with the smallest index
 372 is considered as effective while the others are deemed
 373 duplicates. Then, the polygons with duplicate vertices are
 374 divided into two groups. Those with two or more duplicate
 375 vertices from the same group (i.e. zero-area facets) are
 376 deleted directly, while the others have their duplicate
 377 vertices replaced by the effective vertices of the same
 378 group.

379 After removing all the duplicate vertices and zero-area
 380 polygons, the second step is to build the connectivities
 381 among vertices, line segments and polygons and store all
 382 the neighbors for each primitive. With reference to the
 383 “neighborhood watch” algorithm [16], there are three kinds
 384 of primitives in a mesh: vertices, line segments and
 385 polygons. Thus the concept of *active polygon* is extended
 386 to *active primitive*, the primitive that the HIP is in contact
 387 with. In our paper, we define the *neighbors* for the three
 388 primitive types referring to the definitions in [16]:

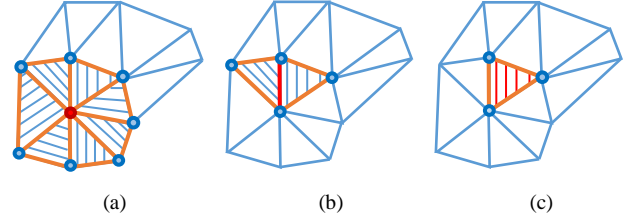
- 389 • For a polygon, the neighbors are its line and vertex
 390 components.
- 391 • For a vertex and a line, their neighbors include all
 392 the polygons connected to it and all the lines and
 393 vertices that comprise these polygons.

394 Fig. 4 illustrates an example of how neighbors are
 395 defined for a vertex, a line segment and a polygon.

396 Based on the connectivities between the vertices and
 397 polygons, the vertex normals are recalculated by summing
 398 up the weighted normal of the neighboring polygons and
 399 normalizing the sum [18] as in (1).

$$400 \quad n_v = \frac{\sum_i \alpha_i * n_{f,i}}{\|\sum_i \alpha_i * n_{f,i}\|} \quad (1)$$

401 Here, the weight is each neighboring polygon’s inner
 402 angle at this vertex. Besides, we also check and store
 403 whether a line is on a convex or concave surface. The lines
 404 with only one adjacent polygon are marked as edges. These
 405 lines may be the edges of the outer contour or the edges of
 406 holes on the surface of the mesh.



407 **Fig. 4 .** A vertex neighbor is marked as a small circle, a line
 408 segment neighbor is marked in orange color and a polygon neighbor
 409 is marked with stripes. (a) The red vertex has 7 polygon neighbors,
 410 14 line segment neighbors and 7 vertex neighbors. (b) The red line
 411 segment has 2 polygon neighbors, 4 line segment neighbors and 4
 412 vertex neighbors. (c) The red polygon has 3 line segment neighbors
 413 and 3 vertex neighbors.

414 In the final preprocessing step, we apply a uniform
 415 partition to the space within the bounding box of the
 416 polygon mesh and divide this space into cells. The size of
 417 the cell is determined by the highest local density of the
 418 mesh. To narrow down the search range for active primitive
 419 and to meet the real-time requirement, the maximum
 420 number of polygons in one cell needs to be constrained. We
 421 identify the largest number of polygons in one cell before
 422 proceeding to collision detection and adjust the cell size
 423 based on this number. In our method, a polygon is
 424 considered as belonging to one cell if a vertex of the
 425 polygon is in this cell, the polygon has an edge intersecting
 426 with the bounding box of this cell or the bounding box of
 427 this cell intersects with the polygon. This criterion is the
 428 same as that in [11].

429 3.3. Collision detection with the preprocessed meshes

430 The challenge of collision detection with large-scale
 431 meshes lies in how to obtain the active polygon in real time
 432 (1000 Hz). The existence of an active primitive is the
 433 necessary and sufficient condition for point-based collision.
 434 As illustrated in Fig. 5, in our method the detection
 435 procedure in the current frame is divided into two branches
 436 based on the collision status in the immediately preceding
 437 frame.

438 If there is no collision between the HIP and the mesh in
 439 the previous frame (*the first branch*), we check whether the
 440 ray from the HIP in the previous frame to that in current
 441 frame intersects with the mesh. The reason behind it is that
 442 when the HIP goes inside of the mesh from outside,
 443 intersection always happens. Therefore, based on the
 444 intersection test result, we further break down this branch
 445 into two sub-branches:

- 446 1. If the ray from the previous HIP to the current HIP
 447 intersects with the mesh at one polygon, this polygon is
 448 treated like the previous active primitive and served as start
 449 point in the tracking for active primitive in the current frame.

445 2. Naturally, if there is no intersection then there is no
 446 collision in the current frame.

447 Correspondingly, if the HIP collides with the mesh in
 448 the previous frame (*the second branch*), then the active
 449 primitive in the previous frame is used as a start point to
 450 track the path of the HIP and locate the active primitive in
 451 the current frame. If the tracking succeeds, it means that the
 452 HIP is still in contact with the mesh in this frame. Otherwise
 453 we consider that the contact has stopped.

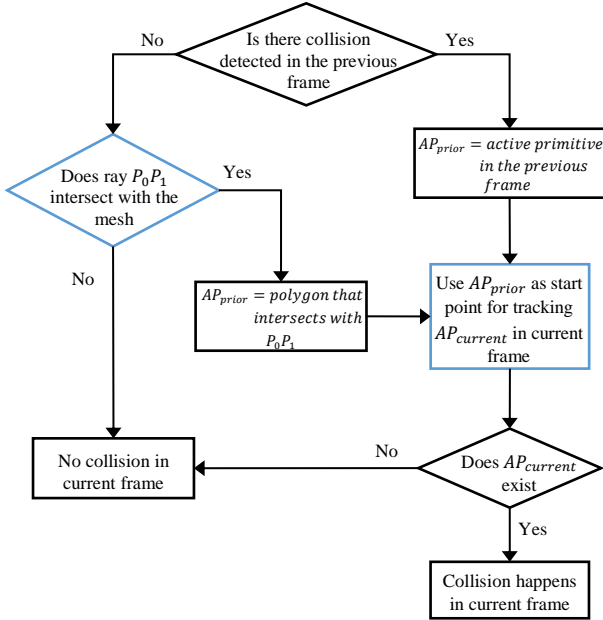


Fig. 5. Flowchart of collision detection process. P_0, P_1 denotes the HIP in the previous and the current frame. AP means active primitive.

454 During the whole process, there are two key modules:
 455 the intersection test between the ray and the mesh and the
 456 tracking of the active primitive (marked blue in Fig. 5).
 457 More implementation details about these two modules are
 458 presented in the following.

3.3.1. Intersection test

460 In our previous paper [3], the collision detection
 461 algorithm is built on the assumption that if the HIP crosses
 462 mesh surface in a frame then the active polygon in this
 463 frame would be in the same cell as the haptic cursor. This
 464 assumption enables us to narrow down the detection range,
 465 however, it does not always hold. When it fails, the
 466 detection would also fail, resulting in unexpected pop-
 467 throughs.

468 To remove this assumption, in this paper we introduce
 469 ray tracing into the first branch of our algorithm,
 470 dismantling this part into an intersection test, which will be
 471 described in the following, and a tracking process, which is
 472 the same as the process run in the second branch but with
 473 different initial values.

474 For the intersection test, the first step is to check
 475 whether the HIP is inside the bounding box of the mesh in
 476 the current frame. If it is inside the bounding box, we
 477 proceed to locate the cell that the HIP is in. Suppose P_0 is
 478 the HIP in the previous frame and P_1 is the HIP in current
 479 frame. If $P_1 \in cell_0$, then based on the connectivity relation
 480 between cells we can find all the cells $\{cell_0, \dots, cell_n\}$ that
 481 the ray P_0P_1 passes through. To find the intersected

482 polygon from these cells, we start with $cell_0$. We check
 483 whether ray P_0P_1 intersects with any of the polygons inside
 484 $cell_0$. If this is the case, we check whether there is an
 485 intersection with polygons inside $cell_1$. We continue like
 486 this until we find the intersected polygon or we reach $cell_n$.
 487 In this way, the computation complexity of the intersection
 488 test is only related to the polygon number inside the cells
 489 along the HIP path.

490 Fig.6 illustrates how we derive all the target cells one
 491 by one. As we can see, P_1 is in cell a and the ray P_0P_1
 492 intersects with the blue polygon at point Q . This intersected
 493 polygon is in cell b, d and e , not in the same cell as the HIP
 494 P_1 . Since cell a does not contain the intersected polygon,
 495 we check whether P_0P_1 intersects with the boundary of cell
 496 a . Since an intersection exists, we locate the intersection
 497 point P_1^1 and update P_1 with it. The location of this
 498 intersection point also determines the common face and
 499 thus the next target cell c . In the same manner, we can
 500 identify cell b based on intersection point P_1^2 and eventually
 501 obtain all the cells $\{a, c, b, e, d\}$ in the listed order.

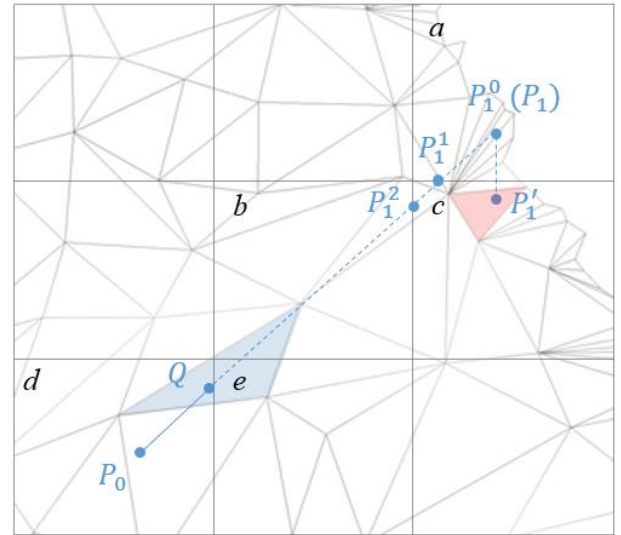


Fig. 6. An example to illustrate how to find all the cells intersected with ray P_0P_1 in the following order: $a \rightarrow c \rightarrow b \rightarrow e \rightarrow d$. The triangle intersected with P_0P_1 is marked blue while the active primitive is marked red. P_1^1 is the projection of P_1 on the active primitive.

502 We note that the existence of an intersected polygon
 503 does not necessarily mean there is collision between the
 504 HIP and the mesh in this frame. Let us consider as an
 505 example the case in Fig. 7. The ray P_0P_1 intersects with
 506 the mesh, but neither P_0 nor P_1 is inside the mesh, i.e. no
 507 collision happens. Therefore, after we obtain the intersected
 508 polygon, we need to use it as start point to track the active
 509 primitive. Only if an active primitive exists can we confirm
 510 that the collision has happened.

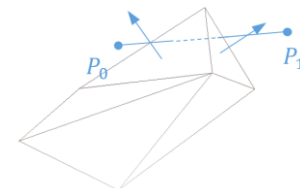


Fig. 7. An example to illustrate difference between intersection and collision.

511 3.3.2. Tracking of the active primitive

512 Based on the geometry connectivities built in
513 preprocessing step, given a start point, we are able to follow
514 the path of the HIP and track the active primitive. This start
515 point can be a polygon, a line segment or a vertex. We refer
516 to it as a *start primitive* in the following. The start primitive
517 can be obtained from two sources: the intersected polygon
518 derived from the intersection test or the active primitive in
519 the previous frame.

520 Three conditions need to be fulfilled to make a primitive
521 active in one frame:

- 522 • **HIP criterion:** the HIP is inside the mesh.
- 523 • **Distance criterion:** this primitive has the shortest
524 distance to the HIP compared to its neighbors.
- 525 • **Projection criterion:** the orthogonal projection of
526 the HIP onto this primitive is inside its range.

527 Considering the relations between these three
528 conditions, we examine them in the following order: firstly,
529 we find the primitive which meets the last two conditions,
530 then we check whether the first condition is true for this
531 primitive.

Algorithm 1 Algorithm for obtaining the active primitive

```

532 activepri_prior ← startprimitive
533
534 repeat
535   activepri_temp ← activepri_prior
536   set A = {activepri_prior, neighbors of activepri_prior}
537
538   for all polygons  $\in A$ ,
539   if there exists a polygon which has the projection of HIP onto it inside its
540   range then
541     distmin =  $\min\{|dist_i| : \text{the projection of HIP on } polygon_i \text{ plane is inside}$ 
542      $polygons_i, polygons_i \in A\}$ 
543     activepri_temp ← polygon with distmin to the HIP
544   else
545     for all line segments and vertices  $\in A$ ,
546     if  $\min\{dist_i : line_i \in A\} < \min\{dist_j : vertex_j \in A\}$  then
547       distmin =  $\min\{dist_i : line_i \in A\}$ 
548       activepri_temp ← line segment with distmin to the HIP
549     else
550       distmin =  $\min\{dist_j : vertex_j \in A\}$ 
551       activepri_temp ← vertex with distmin to the HIP
552     end if
553   end if
554
555 until activepri_temp == activepri_prior
556
557 vector ← vector from HIP to the projection of HIP onto activepri_temp
558 normal ← the normal of activepri_temp
559 if vector * normal < 0 then
560   collision ← FALSE
561 else
562   collision ← TRUE
563   activeprimitive ← activepri_temp
564 end if

```

Fig. 8. Pseudocode of algorithm for obtaining the active primitive.

532 The whole tracking process is represented as a repeat
533 until loop operation in the pseudocode given in Fig. 8. The
534 loop starts with the determined start primitive. In each
535 iteration, AP_{new} is selected from the input primitive
536 AP_{prior} and its neighbors based on the distance and
537 projection criteria for being an active primitive. If AP_{new}
538 is the same as AP_{prior} , it would be considered as a potential
539 active primitive and be checked to find whether it meets the
540 last condition, i.e. the HIP criterion. Otherwise, the loop
541 continues with AP_{new} as the input primitive for the next
542 iteration. A primitive that meets all three criteria is the

543 active primitive in the current frame and it will be saved and
544 used as the start primitive for the tracking in the next frame.

545 In our algorithm, when examining a primitive and its
546 neighbors based on the distance and projection criteria, we
547 incorporate the features of each primitive type into the
548 checking order. For a polygon, if the projection of the HIP
549 is inside its range, then it definitely has the shortest distance
550 to the HIP compared to its components (three line segments
551 and three vertices). The same rule applies to the line
552 segment: If one line segment has the projection of the HIP
553 on it, it certainly has the shortest distance to the HIP
554 compared to its two vertices. Therefore, we calculate and
555 compare the distances of the potential active primitive and
556 its neighbors to the HIP following this order: polygons first,
557 then line segments, and lastly the vertices (reflected in the
558 blue part of Fig. 8).

559 3.4. Force rendering

560 We assume that the interactive models are hard and stiff
561 objects, therefore we apply constraint-based haptic
562 rendering: we compute a proxy to represent the haptic
563 cursor so that the cursor is always visible. When the HIP is
564 moving in free space, the position of the proxy matches the
565 HIP. When there is a collision, the active primitive is
566 known and the proxy is assigned as the projection of the
567 HIP on the active primitive.

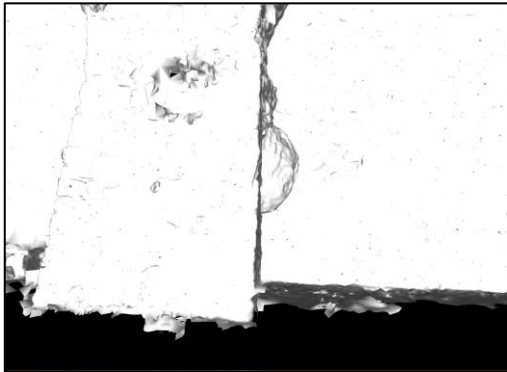
568 We use a spring force model. The magnitude of the
569 force feedback is proportional to the penetration depth of
570 the HIP into the active primitive, which is exactly the
571 *distmin* that we obtain in the iteration loop of Algorithm 1.
572 Normally, the force is computed in the same direction as
573 the facet normal. In our method, we use this approach if the
574 active primitive is a polygon. When the active primitive is
575 a line segment, the force is applied along the direction
576 opposite to the movement, which is from the proxy to the
577 HIP position. In this way, we can effectively prevent the
578 haptic cursor from crossing the edges. Thus, if the cursor
579 slides to a hole on the mesh, it would not fall into the hole.
580 The disadvantage of this strategy is that if the cursor slides
581 along a ragged edge, there are frequent changes in the force
582 direction, since we always give the cursor a resistant force
583 perpendicular to the edge. If the force direction is in the
584 same direction as the velocity, this may lead to a cursor
585 jump.

586 4. Results

587 The images in Fig. 9 illustrate how the concepts
588 introduced in the previous section are implemented given a
589 reconstructed model. Fig. 9(a) shows the original
590 reconstructed city-wall model included in MVE [9], while
591 the small image in the left upper corner is the image to be
592 used for visual display in the interactive scene. Based on
593 the reconstructed camera parameters of this image, we
594 transform the model to the camera workspace and obtain
595 the part in Fig. 9(b) after clipping. We can see that the
596 clipped model matches with the content of the image (Fig.
597 9(c)). After transformation and mapping, the haptic cursor
598 is able to interact with the city wall in the image as
599 displayed in Fig. 9(d). The red ball in Fig. 9(d) represents
600 the proxy of the haptic cursor. A red line pointing to the
601 normal direction is also shown, indicating that the cursor is
602 in contact with the model now.



(a)



(b)



(c)



(d)

Fig. 9. (a) the original reconstructed model. (b) the transformed model displayed in simulated camera frustum. (c) the alignment of the transformed model and the image. (d) a snapshot of the interactive scene.

603 The examples of haptic interaction with the models
 604 reconstructed from images (Fig. 10) can be seen in the
 605 companion video, which is also available at
 606 https://youtu.be/6_tHrG9q3H8. We are able to explore the
 607 scene by switching between consecutive images forming a
 608 walkthrough and touching the image content with the haptic
 609 cursor. With the reconstructed mesh superimposed on the
 610 images, the images are tangible like real 3D scenes. When
 611 the haptic cursor collides with a tangible object in the
 612 image, it always stays on the surface of the object as if it is
 613 interacting with real rigid objects. When the cursor goes to
 614 the back of the object, it would be hidden.



Fig. 10. Examples of interactions with the models reconstructed from images. The cursor is displayed as a red ball in the interactive scenes.

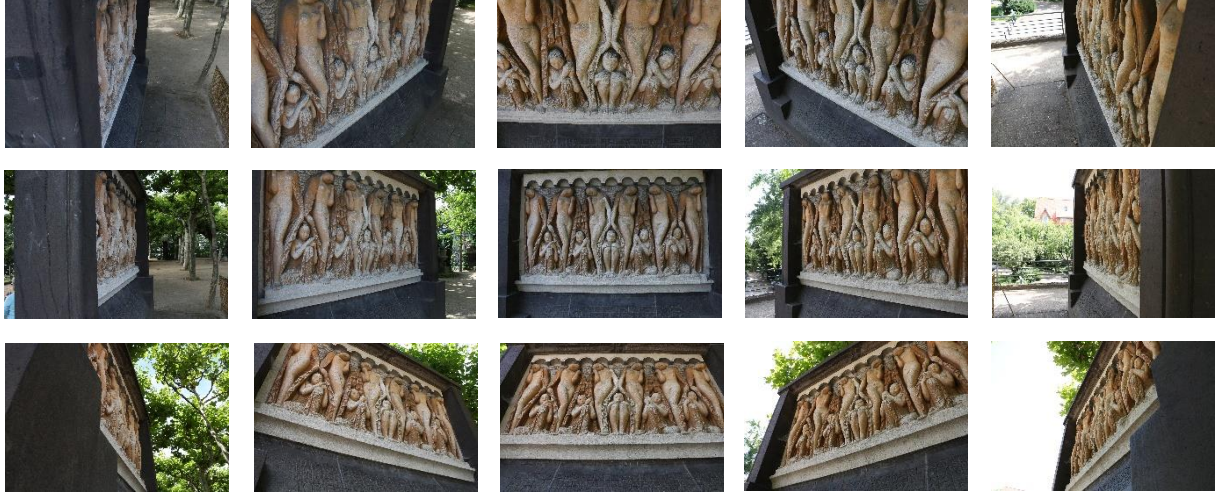


Fig. 11. Top row: photos taken from high viewpoint. Middle row: photos taken from normal eye-level viewpoint. Bottom row: photos taken from low viewpoint.

5. User Study

In our previous paper [3] we conducted the comparison experiment which has shown that the performance of our system far outweighs the commonly-used haptic renderers (God-object renderer [10] provided by H3D API and OpenHaptics HLAPI [13]) in colliding with large-scale meshes. In this paper we report the results of the subjective user tests evaluating what the users think about our approach.

5.1. Capturing test photos

Mathildenhöhe sculpture photos (Fig. 11) used in this test were captured by orbiting a camera around the sculpture center. The camera was incrementally rotated to record the sculpture from different viewing angles. Besides taking photos from normal eye-level viewpoint, we also captured the sculpture from high and low viewpoints. During capturing the camera was always looking at the central part of the sculpture.

Selectively we chose 21 photos from each viewpoint and put them in a 3-row grid to simulate a constrained rotation effect (Fig. 11). All these chosen photos were preloaded to our system before the test.

In the reconstruction of the Mathildenhöhe sculpture model, 256 photos were put into the MVE system, including the photos used in our test. The reconstructed model contained around 5 million triangles.

5.2. Experimental Setup

Our system was run on a computer with CPU working at 2.60GHz. The users were expected to learn the displayed scene by both visual and haptic interaction with it. The visual interaction was supported as a panoramic rotation of the scene controlled by the left and right arrow keys. With each key pressed, the respective next image of the captured scene from the image sequence was displayed. Haptic interaction was implemented using Geomagic Touch desktop haptic device placed close to the user's dominant hand (Fig. 12). The users sat in front of the device and were asked to touch the objects in the scene by moving the haptic cursor displayed in it. The scene could be rotated in 180 degrees counterclockwise to view and touch the objects from different perspective.



Fig. 12. A beta test participant interacts with the tangible photos.

5.3. Experimental Design

5.3.1. Measurements

Table 1

Questions and corresponding factors. These factors are rated on a scale of 1 to 5, where 1 means not at all and 5 means very much.

Question	Factor
How realistic is your haptic interaction with the displayed scenes?	Realism
How well could you actively explore the displayed scenes by touching?	Realism, Sensory
How comfortable do you feel interacting with the displayed scenes?	Comfort
How useful is the haptic feedback in improving your interaction experience?	Sensory
How satisfied are you with your interaction experience?	Satisfaction

A questionnaire as in Table 1 was designed to evaluate interaction with tangible images. Based on Presence [19], four Factors are evaluated in this questionnaire: realism, sensory, comfort and satisfaction.

662 Among the five questions, the second question
 663 contributes to two factors. According to [19], the
 664 correlation coefficient of this question is 0.15. Thus we
 665 computed the results for realism and sensory in this way:

$$666 \quad \text{realism} = 0.15 * Q2 + 0.85 * Q1 \quad (7)$$

$$667 \quad \text{sensory} = 0.15 * Q2 + 0.85 * Q4 \quad (8)$$

668 5.3.2. Procedures

669 24 users participated in our test, 7 female and 17 male.
 670 1 participant was ambidextrous and tried our system with
 671 both hands. 17 of them never used any haptic device. The
 672 entire test took 20 to 30 minutes to complete. Here are
 673 detailed procedures:

- 674 1. Demonstration of how to use Geomagic Touch with
 675 an example. Proper training is necessary before the
 676 test to eliminate the tension of the users, especially
 677 for novices.
- 678 2. User testing. The users were asked to explore the
 679 displayed image scene with the haptic device.
 680 Viewpoints and viewing angle can be changed by
 681 pressing arrow keys.
- 682 3. Filling in the questionnaire.
- 683 4. Collection of oral feedback. This step is for gaining
 684 a more comprehensive understanding of the ratings.
 685 Their answers are recorded on the questionnaire
 686 during the collection.

687 5.4. Results

688 The results of the questionnaire are shown in Table 2.
 689 The goal of this user test is to know what users think of our
 690 system, and more specifically, to assess the likelihood that
 691 users would accept and want to use our system. We can see
 692 from the table that the means for the four factors were all
 693 above 3 (neutral), which reflects a positive attitude towards
 694 the system. If we calculate the true population means, the
 695 results are still positive. Let us consider realism, the factor
 696 with the lowest mean, as an example. The 95% confidence
 697 interval for its mean 3.46 is 3.05 to 3.87, of which the lower
 698 bound is still slightly higher than 3 (neutral).

Table 2

Results of the questionnaire. These factors are rated on a scale of 1 to 5, where 1 means not at all and 5 means very much.

Factor	Mean	Standard deviation	95% Confidence Interval
Realism	3.46	0.98	0.41
Comfort	3.58	1.14	0.48
Sensory	3.64	0.90	0.38
Satisfaction	3.58	1.02	0.43

699 5.5. Discussion

700 Comments from users are categorized into four groups.

701 5.5.1. Pleasure

702 Most users found it impressive to feel the depth of the
 703 object in the photo, especially when experiencing significant
 704 changes in depth, e.g., sliding from a platform away from us
 705 to one closer to us (as in Fig. 13). Besides, we got comments

706 that they enjoyed this user test and would like to try our
 707 system again.



Fig. 13. Example of sliding from far surface to near surface. The haptic cursor trace is marked with cursor sample points (sampled at 20 Hz), which are represented as red balls. The red line always points to the force direction.

708 5.5.2. Force feedback

709 Most users encountered problems while sliding the
 710 cursor on the surface of small structures with large
 711 curvature, because they found it hard to constrain the cursor
 712 to the surface. Two of them suggested that we should
 713 provide a zooming operation so that they could touch small
 714 details better. Another user compared this phenomenon to
 715 the real life situations and explained it as lack of automatic
 716 assistant force from the wrist which we obtain when sliding
 717 our figure on a real curve.

718 Six users expected to feel the physical properties of the
 719 objects in the interaction, e.g., stiffness, friction, texture and
 720 viscosity. Constrained by the device, it is impossible to
 721 simulate interaction with rigid bodies, but in the future we
 722 could make force feedback more realistic by adding haptic
 723 texture and viscosity to the models and applying friction
 724 based on the real material properties.

725 Another interesting finding from the users' feedback is
 726 that most of them believe that there is too much roughness
 727 at some places which are supposed to be smooth. This may
 728 reflect an unconscious relation between visual feedback and
 729 haptic feedback. The users have an expectation about what
 730 the haptic feedback should be like based on what they see
 731 in the photos. If they do not visually perceive the details that
 732 they are touching, they are likely to deny these details and
 733 interpret them as unexpected roughness. This partially
 734 explains why the average rating on realism is just mediocre
 735 (3.46 on a scale of 1 to 5). Based on this, we conclude that
 736 such a system should not provide haptic details that cannot
 737 be perceived by eyes. In addition, the force should be
 738 smoothed so that the users do not get frustrated because the
 739 HIP is stuck at small surface details.

740 5.5.3. Device

741 Five users pointed out that they felt tired or
 742 uncomfortable holding the handle for a prolonged time and
 743 three of them explicitly wrote that this has negative
 744 influence on their ratings for satisfaction. We could not
 745 change the ergonomics of the device but there could be
 746 some ways to improve the comfort level, e.g., using some
 747 form of cushioning or support for the hand.

Another complaint about the device is that it is not so intuitive, which results from limited force output and only one interaction point. These are limitations of such ground-based haptic interfaces. If we replace the device with body-based haptic interfaces such as gloves, suits and exoskeletal devices, the user experience could be improved to some extent, but the cost would also increase largely.

5.5.4. Usefulness

Most users showed reserved positive attitude towards the usefulness of the haptic feedback in interaction with photos. Only three out of twenty-four users gave negative feedback.

Those who gave positive or neutral feedback believed that having one more dimension of feedback is better than simply viewing the photos. They commented that this system could be useful for people with bad depth perception or if the photo content involves unclear structure. One user also mentioned an inspiring observation: her memory about photos is largely enriched in this way and she can remember the content of the photos better after touching them.

5.5.5. Others

Before the test, we did not inform the users which part of the photos is tangible, so they need to explore it themselves. Three users found that only the sculpture part is tangible and commented that they also wanted to touch other objects in the photo background, e.g., trees, houses and cars. Therefore, one of our goals in the future is to make the whole photo tangible or to think of a way to communicate to the users which parts are tangible.

Moreover, we noticed that two users were confused about what touching feels like at the beginning of the test. After our explanation they knew that seeing the haptic cursor does not indicate the occurrence of contact with the objects in the scene. They would feel the haptic feedback only when reaching the depth of the object with the cursor. This confusion is due to the fact that people are not used to derive depth information in the virtual environment without reference. Therefore, additional training about what it means to touch might be necessary and assistive visual feedback could be helpful.

6. Conclusion

We have presented our approach to creating tangible images using models reconstructed by multi-view vision techniques. To deal with large-size, partially dense reconstructed meshes, we propose an improved hybrid collision detection method. By preprocessing the mesh with uniform partitioning and building connectivities among the vertices, lines and polygons, we are able to handle collision detection with meshes of over ten million triangles.

In this approach, we align the haptic models with the images so that the haptic display would match the visual content. Occlusion of the haptic cursor is simulated as if it was interacting with a real 3D scene.

With the presented method, we add a new modality into interaction with images. Besides viewing an image, this method enables us to appreciate the image content within a touching distance and complements our viewing experience.

Despite the limitations of the device (i.e. not so intuitive, feeling uncomfortable if holding the handle for long time), the results of the usability test show that we have provided

an enjoyable and easy way to enrich images with a touch interface and haptic feedback. Based on the users' comments, there are many things that can be improved (e.g., adding haptic texture and viscosity to the models), but generally this new approach meets the users' expectation about haptic interaction and it brings new possibilities into interaction with images.

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